



resonant frequencies in the low-speed and high-speed axes of 30Hz and 600 Hz has not yet been reported.

This study aims to develop silicon micro-mirrors with two asymmetrical axes for electrostatic field distribution measurements using a single external piezoelectric ceramic vibrating element. The vibration transmissibility of the proposed mirror under a vacuum atmosphere was evaluated by dynamic analysis. We measured an electrostatic field distribution using the 2D asymmetric silicon micro-mirrors by means of the optical level method.

## 2. Design and vacuum-sealing package

### 2.1 2D asymmetric silicon micro-mirror design

To evaluate the absolute deformational displacement of the characteristic mode, we conducted simulated modal analysis of the resonance frequency and dynamic analysis. The resonance frequency of the 2D asymmetric silicon micro-mirror was evaluated using the IntelliSuite software (IntelliSuite, ver. 8.7).

We designed 2D asymmetric silicon micro-mirrors, as shown in Fig. 1. The 2D asymmetric silicon micro-mirrors were designed to be 5.8 mm long  $\times$  5.8 mm wide  $\times$  15  $\mu$ m thick. The torsion mirror was 1.7 mm long  $\times$  2.0 mm wide.

First, we used Blueprint, which is a physical design tool. The 3D model was constructed in IntelliSuite's 3D builder, which is a 3D mesh generator. The frequency analysis was performed by using the ThermoElectroMechanical analysis module. The minimum mesh was 46  $\mu$ m long  $\times$  2.5  $\mu$ m wide  $\times$  7.5  $\mu$ m thick at torsion. The parameters used in the analysis are summarized in Table 1.

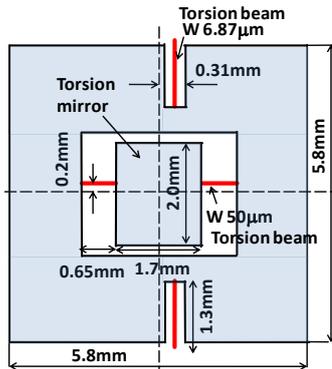


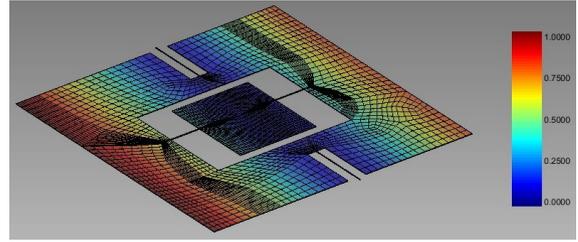
Fig. 1. Layout of a 2D asymmetric silicon micro-mirror.

Table 1. Parameters used for analysis with the IntelliSuite software

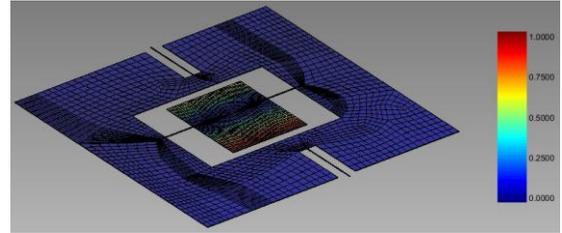
Material	Silicon
Young's modulus	160 GPa
Density	2.30 g/cm <sup>3</sup>
Poisson's ratio	0.226

In the first stage, we performed the modal analysis using the IntelliSuite software. Fig. 2 shows the results of the modal analysis of the 2D asymmetric silicon micro-mirrors. The resonance frequencies in the low- and high-speed axes, as calculated by the ThermoElectroMechanical module of the IntelliSuite software package, were 30 Hz and 604 Hz, respectively. The results indicate the eigenvalue and mode shape. However, dynamic analysis is necessary to evaluate the absolute deformational displacement of the characteristic mode. The dynamic analysis can indicate the absolute amount of modification

although the modal analysis can evaluate the relative spatial relationship of modification.



(a) Low-speed axis (Normalized modal displacement of Mode 1:30.708Hz)



(b) High-speed axis (Normalized modal displacement of Mode 6:604.48Hz)

Fig. 2. Modal analysis of 2D asymmetric silicon micro-mirrors.

Fig. 3 shows the model for dynamic analysis of the 2D symmetric silicon micro-mirrors. The sine wave amplitude was generated by a pressure of 0.1 MPa as a function of frequency, although the mesh size differs from that used in the modal analysis. Fig. 4 shows a plot of the amplitude–frequency characteristics calculated by dynamic analysis. The ratio of the deformation between the low-speed axis of 30 Hz and the high-speed axis of 604 Hz was simulated to be 4.04.

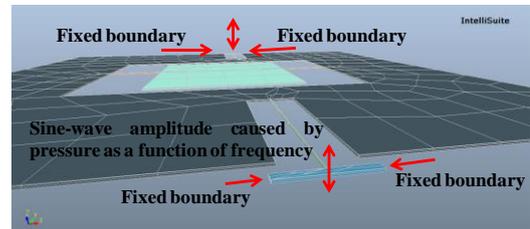


Fig. 3. Model for dynamic analysis of 2D asymmetric silicon micro-mirrors.

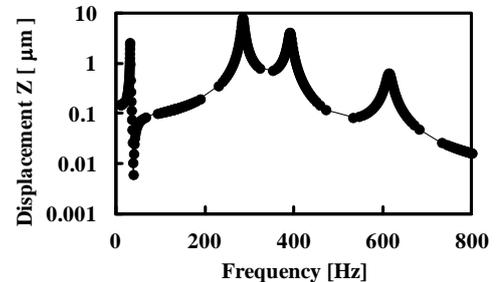


Fig. 4. Vibration transmissibility characteristics calculated by dynamic analysis.

### 2.2 Vacuum-sealing packaging

2D asymmetric silicon micro-mirrors were fabricated by SOI-MEMS process<sup>(11)</sup>; a photograph of one of the resulting micro-mirrors is shown in Fig. 5 (MEMS CORE). The torsion

beam was cut with a picosecond-laser micromachining system (Japan Laser and Time-Bandwidth, Duettino-SHG). For micromachining with a picosecond laser, the 2D asymmetric silicon micro-mirror was placed on a 2D nano-motion stage (Aerotech, ANT130-160), which was driven by motion controlled software (Aerotech, Automation 3200).

After the 2D asymmetric silicon micro-mirror was placed on the piezoelectric ceramic vibrating element, we adhered the 2D asymmetric silicon micro-mirror to the piezoelectric ceramic vibrating element and vacuum-sealing package (KYOCERA) which was vacuumed to the degree of  $5 \times 10^{-3}$  Pa. Fig. 6 shows a photograph of the vacuum-sealed package with the embedded 2D asymmetric silicon micro-mirror.

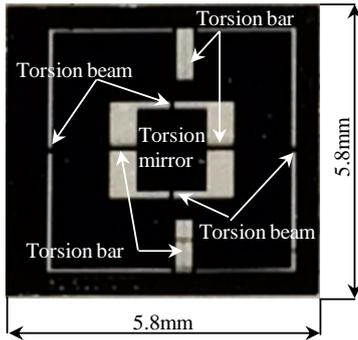


Fig. 5. Photograph of the asymmetric silicon micro-mirror fabricated by the SOI-MEMS process, which is made from the silicon-on-insulator by the semiconductor process.

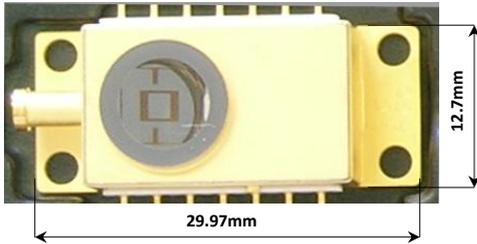


Fig. 6. Photograph of the vacuum-sealed 2D asymmetric silicon micro-mirror.

### 3. Results

#### 3.1 Scanning characteristics of the 2D asymmetric silicon micro-mirror

Fig. 7 shows a photograph of the experimental setup of the vacuum-sealing package. We obtained the resonant frequency in the low-speed axis of 23.3 Hz and in the high-speed axis of 556.8 Hz respectively. To prevent a reduction in the amplitude width, we induced a  $90^\circ$  phase shift between the low- and high-speed axes at the resonance frequency, as shown in Fig. 8. In measurement, the ratio of the deformation between the low-speed axis of 23.3 Hz and the high-speed axis of 556.8 Hz was 6.48. A photograph of the Lissajous pattern projected onto a screen of 300 mm away from the vacuum-sealing package is shown in Fig. 9. We measured the scanning range from the Lissajous pattern with scale. The scanning angle was  $7.6^\circ$  (total angle) in the low- and high-speed axes and was limited by the output voltage saturation of the excited instrument in the vacuum-sealing mount.

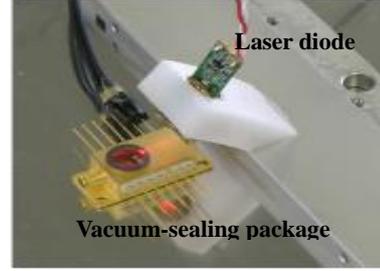


Fig. 7. Experimental setup of the vacuum-sealing package.

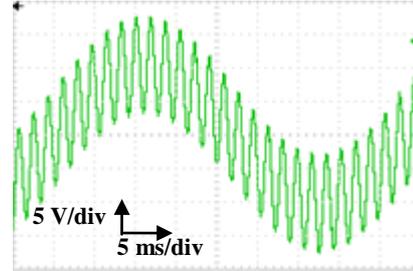


Fig. 8. Digital oscilloscope recording of the drive voltage for the asymmetric silicon micro-mirror shown in Fig. 5 (low frequency: 23.3 Hz, AC 21 Vp-p; high frequency: 556.8 Hz, AC 15 Vp-p).

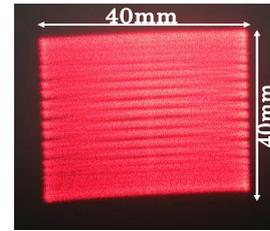


Fig. 9. Photograph of the Lissajous pattern projected onto a screen.

#### 3.2 Electrostatic field distribution measurements

Electrostatic field distribution measurement using a silicon micro-mirror array by SOI-MEMS processes has been reported<sup>(11)</sup>. Fig. 10 shows the schematic of a silicon micro-mirror for electrostatic field distribution measurement.

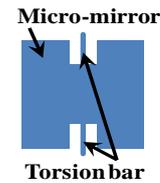


Fig. 10. Schematic of a silicon micro-mirror for electrostatic field distribution measurement

Fig. 11 shows the schematic of electrostatic field distribution measurement using optical level method. When the micro-mirror is moved by electrode, the deflection angle of the torsion mirror by electrostatic force was determined by the method of Peterson<sup>(12)</sup>. The deflection angle of the silicon micro-mirror is given by (1)

$$\phi = \frac{\epsilon_0 V^2 l b^3 (1 + \nu)}{16 K E d^2 t^4} A, \quad (1)$$

where  $\phi$  is the deflection angle of the silicon micro-mirror,  $\epsilon_0$  is dielectric constant of vacuum,  $V$  is applied voltage,  $l$  is torsion bar length,  $b$  is mirror width,  $\nu$  is Poisson's ratio,  $K$  is a constant defined by the shape of the torsion bar. In the case of the torsion

bar with a rectangular cross section,  $K$  is 0.141.  $E$  is Young's modulus,  $d$  is distance between the mirror and voltage-applying electrode,  $t$  is torsion bar width and thickness, and  $A$  is a correction factor determined using the effective electrode area. By substituting the material constant and sizes of the torsion mirror into eq. (1), the relationship between the deflection angle  $\phi$  and applied voltage at the electrostatic field is given.

Fig. 11 shows the schematic of electrostatic field distribution measurement using optical level method. When  $\theta$  is measured using the optical level method, the electrostatic voltage can be calculated from eqs. (1).  $\theta$  can be calculated by measuring displacement  $\Delta d$ .

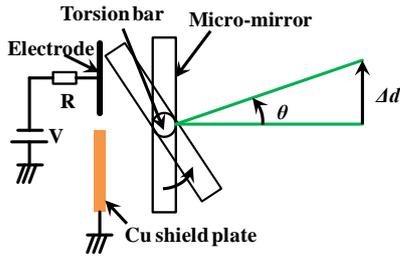


Fig. 11. Schematic of electrostatic field distribution measurement using optical level method

Fig. 12 shows the schematic of the optical measurement setup. The deflection angle of each silicon micro-mirror, which was placed on a spherical surface such as Fresnel lens and was deflected by an electrostatic field, was measured optically using a 2D optical scanner and position-sensitive detector (PSD). A laser beam ( $\lambda = 532$  nm, output power 5 mow, Shimadzu, BEAM MATE) was focused on the silicon micro-mirror and scanned two-dimensionally; the beam then irradiated each micro-mirror through a beam splitter and a convex lens. The reflected laser was reflected by the beam splitter and was focused on the PSD (Hamamatsu Photonics, S1880) surface to allow measurement of the spot position. The horizontal and vertical operations of 23.3 Hz and 556.8 Hz signals, respectively, at the resonance frequency of the asymmetric silicon micro-mirror were driven by the piezoelectric ceramic vibrating element.

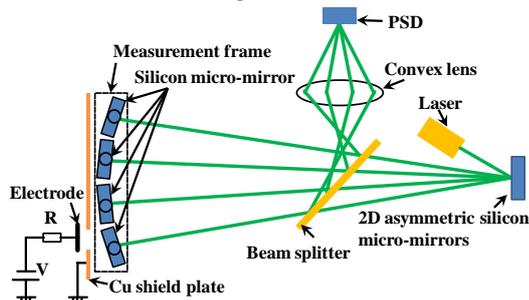
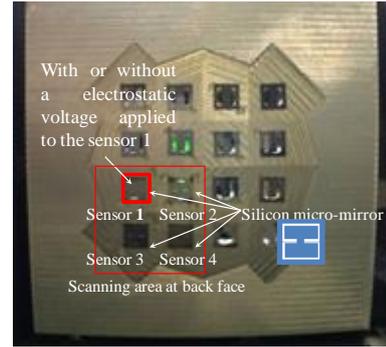
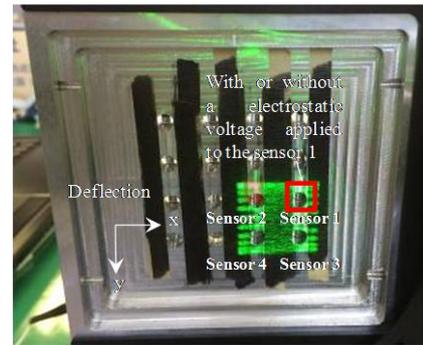


Fig. 12. Schematic of the optical measurement setup.

Fig. 13 shows the photograph of the measurement frame incorporating a silicon micro-mirror array. Sixteen silicon micro-mirrors were attached to the measurement frame. Four silicon micro-mirrors were scanned by a laser beam. The deflection direction was limited to the y-axis. Sensor 1 was with or without an electrostatic voltage applied.



(a) Front



(b) Back

Fig. 13. Measurement frame incorporating a silicon micro-mirror array.

Fig. 14 shows the PSD output signal ( $Y$ ), which was measured by scanning a laser beam across a silicon micro-mirror array at Sensor 1 under an applied electrostatic voltage of 1000 V. The repetition time of 42.9 ms corresponded to the 23.3Hz vertical operation frequency of the 2D asymmetric silicon micro-mirrors. Four spike-like waveforms were observed in the 42.9 ms period. We observed the change in the waveform of the PSD output signal ( $Y$ ) with or without an applied electrostatic voltage of 1000 V by the deflection of the silicon micro-mirrors of Sensor 1, as shown in Fig. 15. Fig. 15(a) shows the waveform at 23.3 Hz. Fig. 15(b) shows the change in waveform under an applied electrostatic voltage of 1000 V applied. Nine peaks were observed.

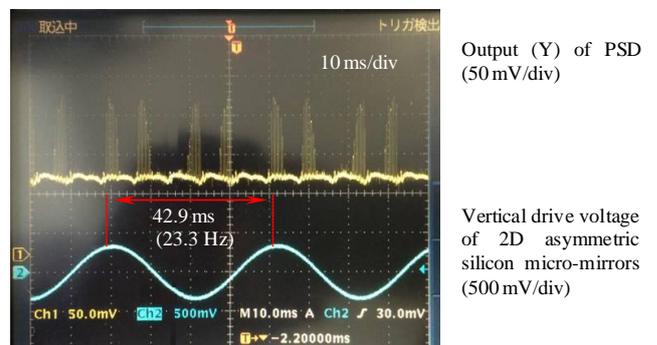
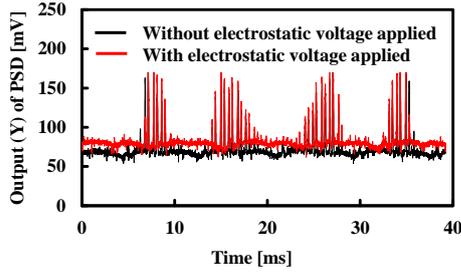
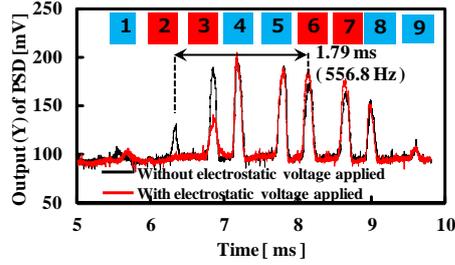


Fig. 14. Photograph of the output signal of the position-sensitive detector (PSD).



(a) Waveform at 23.3 Hz



(b) Change in waveform

Fig. 15. Measurement output (Y) of the position-sensitive detector (PSD) with or without the electrostatic voltage applied.

#### 4. Discussion

In this study, we developed silicon micro-mirrors with two asymmetric axes for electrostatic field distribution measurements. The vibration transmissibility of the proposed mirror under a vacuum atmosphere was evaluated by dynamic analysis. We measured the electrostatic field distribution using our fabricated 2D asymmetric silicon micro-mirrors.

The ratio of the deformation between the low-speed axis of 30 Hz and the high-speed axis of 604 Hz was simulated to be 4.04. In measurement, the ratio of the deformation between the low-speed axis of 23.3 Hz and the high-speed axis of 556.8 Hz was 6.48. The difference between the calculated and experimental values was apparently due to fabrication errors and the frequency characteristics of external piezoelectric ceramic vibrating element.

In the case of the 2D silicon scanning micro-mirrors, to prevent a reduction in the amplitude width, which is caused by interference between the vibrations of the low- and high-speed axes, these axes oscillated in and out of phase with the resonant frequency, respectively<sup>(13)</sup>.

We measured the electrostatic field distribution using the 2D asymmetric silicon micro-mirrors (Figs. 14 and 15). Fig. 16 shows a schematic of the line scan on the measurement frame. The laser beam was scanned in the direction of the arrow from the starting point to the turning point and then returned from the turning point to the starting point. The laser beam scanned Sensors 1 and 2 four and five times, respectively. The turns are labeled with the notation of 1 to 9 in Fig. 16. When the electrostatic voltage of 1000 V was applied at Sensor 1, the output of the PSD (Y) changed. The measurement outputs (Y) of the PSD with the notations of 2 and 3 decreased, whereas those of 6 and 7 increased.

The PSD can be used to measure the position of the light spot on its surface from each current of four electrodes<sup>(14)</sup>. The signal was amplified using an operational amplifier and showed a good S/D

ratio. Displacement  $p$  is calculated according to eq. (2) using each electrode current output  $X_1$ ,  $X_2$ ,  $Y_1$ , and  $Y_2$ :

$$p = \frac{X_2 - X_1 + Y_2 - Y_1}{X_2 + X_1 + Y_2 + Y_1} \cdot \frac{L}{2}, \quad (2)$$

where  $L$  is the lateral length of the PSD surface.

Because the deflection direction was limited to the y-axis in our experiments,  $X_2 = X_1 = 0$ . Therefore, eq. (2) becomes eq. (3):

$$p = \frac{Y_2 - Y_1}{Y_2 + Y_1} \cdot \frac{L}{2}. \quad (3)$$

Fig. 17 shows a schematic of the output of the PSD (Y) change with or without an applied electrostatic voltage. When the micro-mirror was deflected with an electrostatic voltage, the laser spot on the surface of the PSD moved from its initial point without an electrostatic voltage. The displacement changed as shown in eq. (3). In the case of the measurement output (Y) of the PSD with the notations of 2 and 3 (Figs. 15 and 16), the displacement becomes negative from the initial position. In the case of the measurement output (Y) of PSD with the notations of 6 and 7, the displacement becomes positive from the initial position.

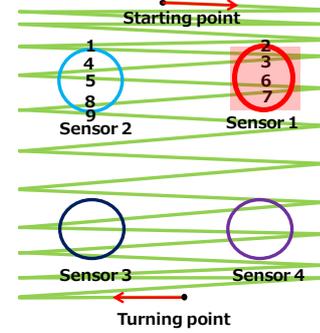


Fig. 16. Schematic of the line scan on the measurement frame.

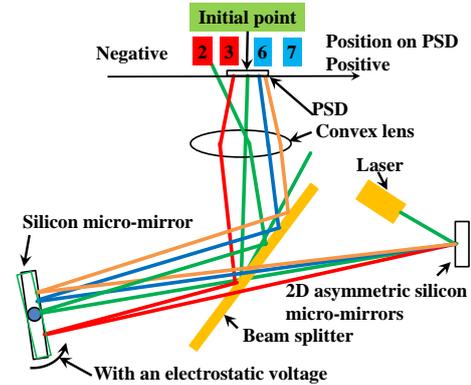


Fig. 17. Schematic of the output of the PSD (Y) change with or without an electrostatic voltage.

#### 5. Conclusions

We developed silicon micro-mirrors with two asymmetric axes for electrostatic field distribution measurements using a single external piezoelectric ceramic vibrating element. 2D asymmetric silicon micro-mirrors were fabricated using an SOI-MEMS process. The vibration transmissibility of the proposed mirror under a vacuum atmosphere was evaluated by dynamic analysis. We obtained the resonant frequency in the low-speed axis of 23.3 Hz and in the high-speed axis of 556.8 Hz respectively. To prevent a

reduction in the amplitude width, we induced a 90° phase shift between the low- and high-speed axes at the resonance frequency. The ratio of the deformation between the low-speed axis of 30 Hz and the high-speed axis of 604 Hz was simulated to be 4.04. In measurement, the ratio of the deformation between the low-speed axis of 23.3 Hz and the high-speed axis of 556.8 Hz was 6.48. The difference between the calculated and experiment values was apparently due to the fabrication errors and frequency characteristics of external vibrating element piezoelectric ceramic vibrating element. A Lissajous pattern projected onto the screen. The scanning angle was a degree of 7.6 (total angle) in the low- and high-speed axis. We subsequently measured the electrostatic field distribution using the 2D asymmetric silicon micro-mirrors.

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